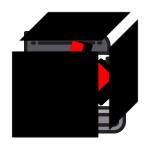
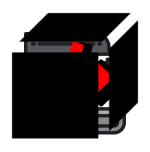
Active Automata Learning Formal Methods for Efficient Model Inference

28/11/2024





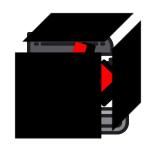




Testing?

Verification?

Understanding?

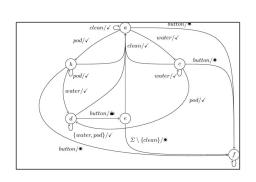


Testing?

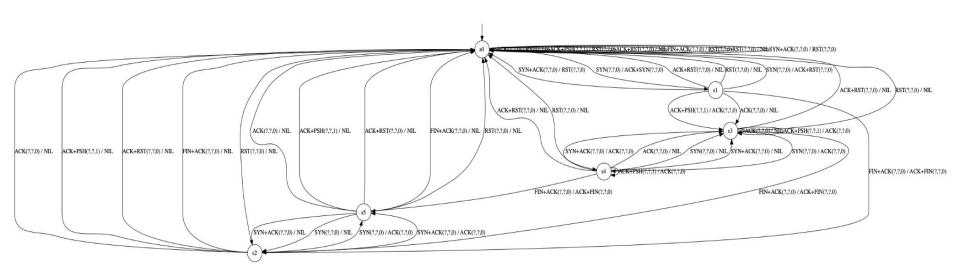
Verification?

Understanding?

Use Automata to
Represent the System
(Explainable and Readable)



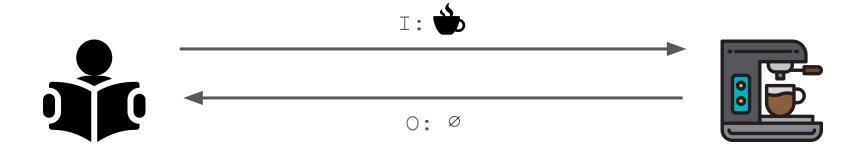
Motivation of Black-Box Automata Learning - Example



A high-level overview



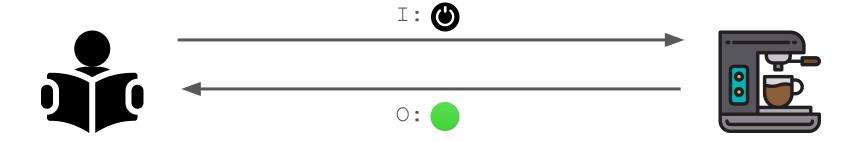










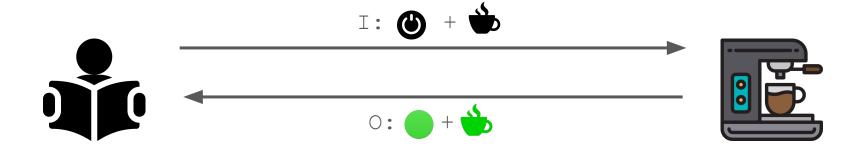








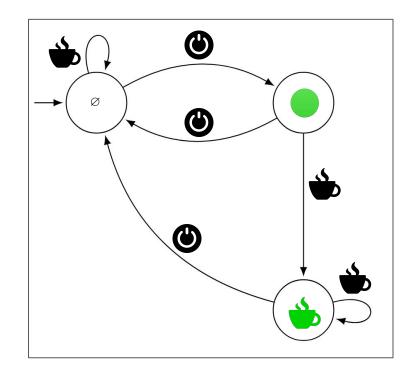




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© ©	Ø
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Back to Basics: DFA

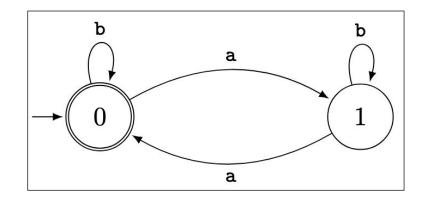
A deterministic finite automaton M is a tuple $(Q, q_0, \Sigma, \delta, F)$, where:

- Q is a finite set of states
- $q_0 \in Q$ is an initial state
- Σ is an alphabet
- $\delta: Q \times \Sigma \to Q$ is a transition function
- $F \subseteq Q$ is a set of final/accepting states

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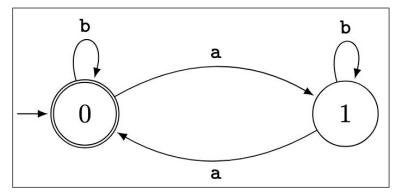
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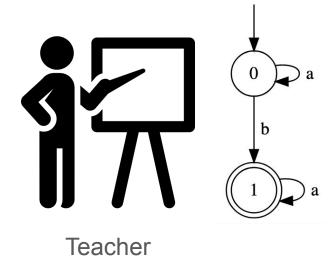
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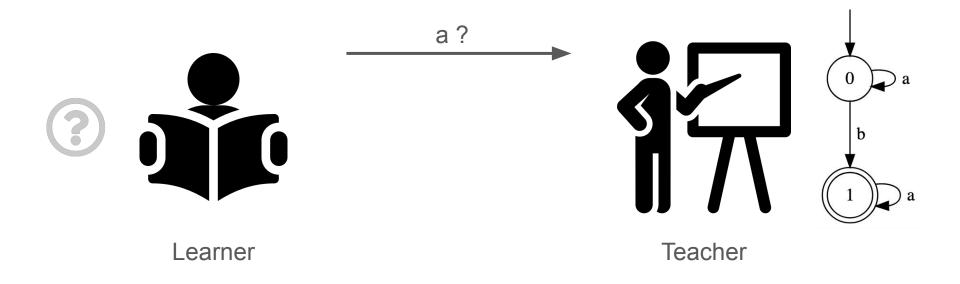
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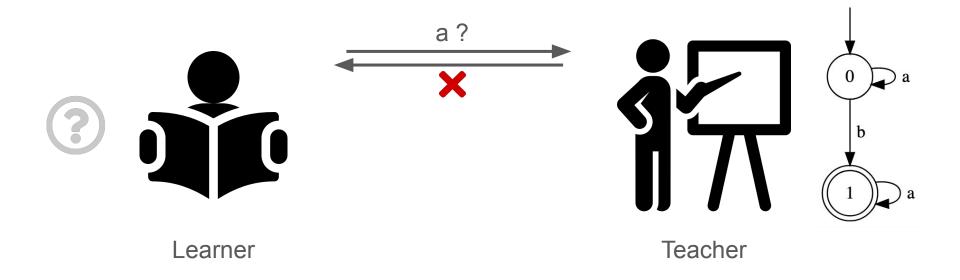


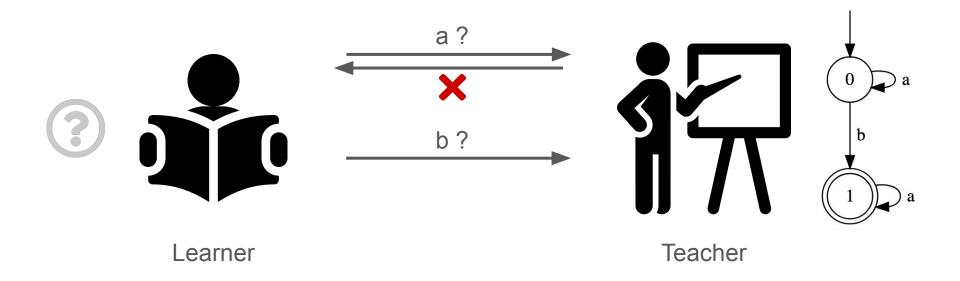
* missing transitions lead to sink state

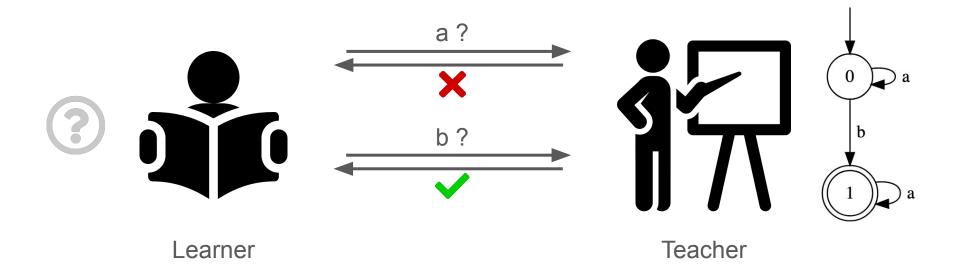




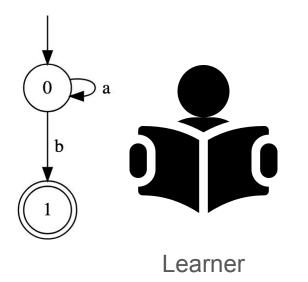


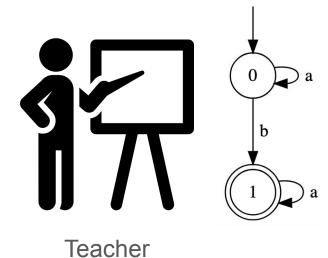




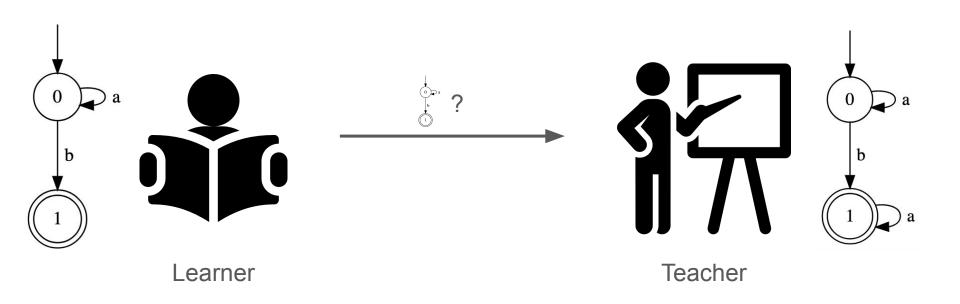


Hypothesis

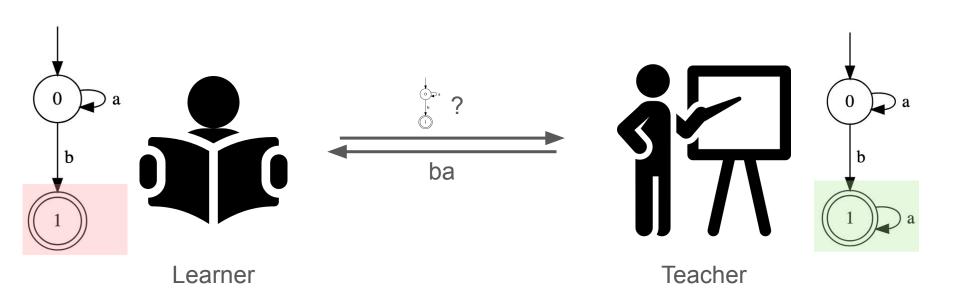




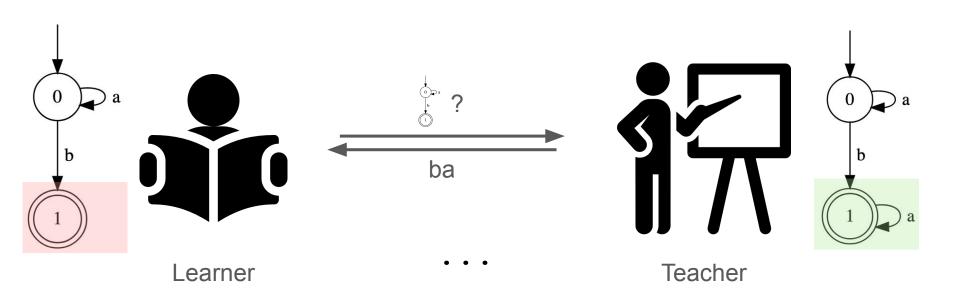
Equivalence Query



Equivalence Query



Equivalence Query



MAT: Observation Table

An observation table is a tuple (S, E, T), where:

- S, E are non-empty finite sets of strings
- T is a mapping $((S \cup S \cdot \Sigma) \cdot E) \to \{\top, \bot\}$

The table structure can be represented visually as:

	E
S	
$S \cdot \Sigma$	

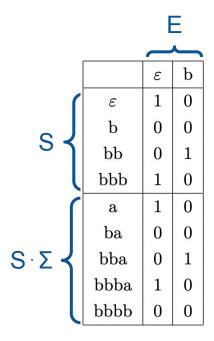
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Example. $\Sigma = \{a, b\}$

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The table structure can be represented visually as:

	$oxed{E}$
S	
$S\cdot \Sigma$	

$$row(\varepsilon) = 1 \ 0$$

 $row(b) = 0 \ 0$
 $row(\varepsilon) = row(bbb)$

ε	b
1	0
0	0
0	1
1	0
1	0
0	0
0	1
1	0
0	0
	1 0 0 1 1 0 0

Example. $\Sigma = \{a, b\}$

MAT: Table to Hypothesis

When an observation table is closed and consistent, we can define a minimal DFA where:

$$Q = \{row(s) : s \in S\}$$

$$F = \{row(s) : s \in S \land T(s) = 1\}$$

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ε	1	0
\mathbf{a}	0	1
aa	1	1
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$$\mathsf{start} \to \hspace{-1.5cm} \begin{array}{|c|c|}\hline \epsilon \end{array}$$





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$$\mathsf{start} \to \hspace{-1.5cm} \left(\hspace{0.5cm} \epsilon \hspace{0.5cm} \right)$$

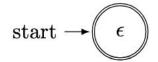




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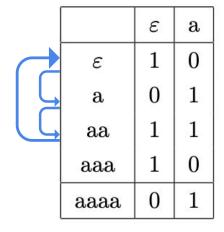


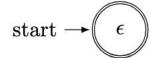




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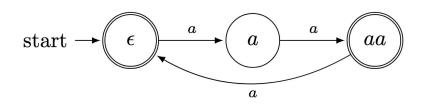




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An observation table is *closed* when $\forall s_1 \in S \cdot \Sigma : \exists s_2 \in S : row(s_1) = row(s_2)$.

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b	0	1
a	1	1
ba	0	1
bb	0	0

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The rows in $S \cdot \Sigma$ not in S are added to S and the table is extended.

	ε	\mathbf{a}
ε	1	1
b	0	1
a	1	1
ba	0	1
bb	0	0

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	ε	\mathbf{a}	ε	
Ξ	1	1	 b	(
b	0	1	bb	0
\mathbf{a}	1	1	a	1
a	0	1	ba	0
bb	0	0	bba	1
			bbb	(
			I.	1

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					ε	
	ε	a		ε	1	Г
arepsilon	1	1	→	b	0	
b	0	1		bb	0	
\mathbf{a}	1	1		a	1	
ba	0	1		ba	0	
bb	0	0		bba	1	
,	1			bbb	0	

$$\forall s_1, s_2 \in S, a \in \Sigma : row(s_1) = row(s_2) \rightarrow row(s_1 \cdot a) = row(s_2 \cdot a).$$

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	ε	a
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\mathbf{a}	1	1
b	1	0
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	ε	a
ε	1	1
\mathbf{a}	1	1
b	1	0
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	ε	\mathbf{a}	
ε	1	1	
\mathbf{a}	1	1	
b	1	0	
ba	0	0	
aa	1	0	
ab	1	0	
bb	0	0	

	ε	a	aa
ε	1	1	1
\mathbf{a}	1	1	0
b	1	0	0
ba	0	0	0
aa	1	0	1
ab	1	0	0
bb	0	0	0

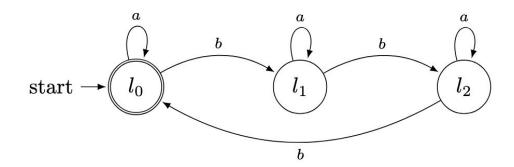
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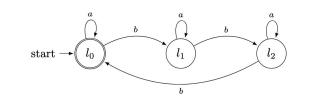
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\mathbf{a}	1	1
b	1	0
ba	0	0
aa	1	0
ab	1	0
bb	0	0

	ε	a	aa
ε	1	1	1
\mathbf{a}	1	1	0
b	1	0	0
ba	0	0	0
aa	1	0	1
ab	1	0	0
bb	0	0	0

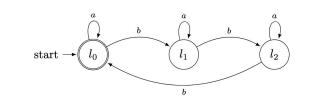
Now a learning example!

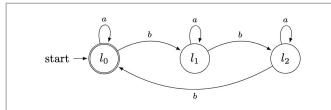




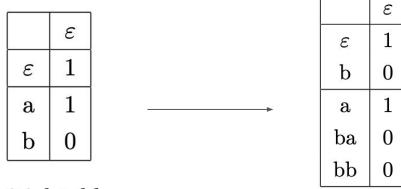
ε
1
1
0

Initial table



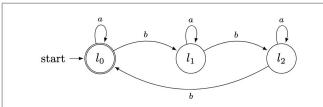


DFA that accepts strings with a number of b multiple of 3

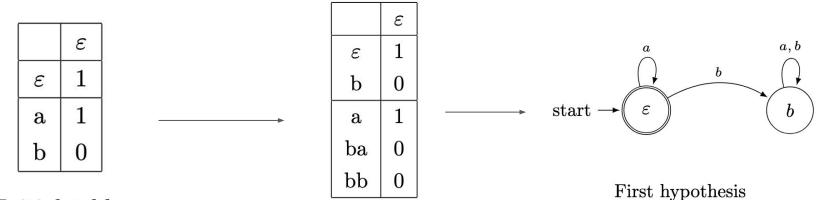


Initial table

Closed (and consistent)

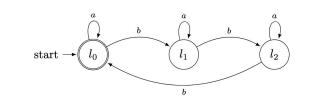


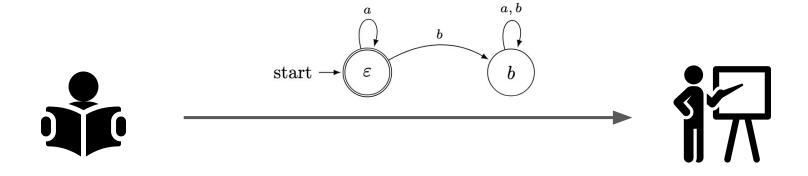
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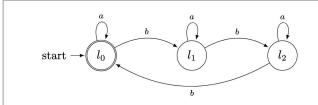


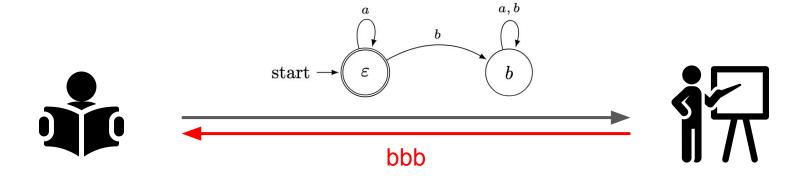
Initial table

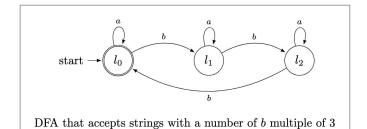
Closed (and consistent)









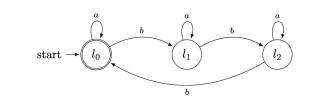


 $\begin{array}{c}
 & \text{start} \longrightarrow \mathcal{E} \\
 & \text{b} \\
 & \text{bbb}
\end{array}$

Add counterexample (and all its prefixes) to S

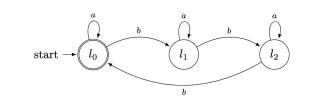
	2
	ε
ε	1
b	0
bb	0
bbb	1
a	1
ba	0
bba	0
bbba	1
bbbb	0

Extended with cex



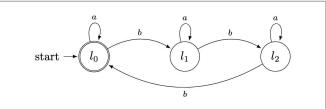
ε
1
0
0
1
1
_
0
-
0

Extended with cex



	ε
ε	1
b	0
bb	0
bbb	1
a	1
ba	0
bba	0
bbba	1
bbbb	0

	ε	b
ε	1	0
b	0	0
bb	0	1
bbb	1	0
a	1	0
ba	0	0
bba	0	1
bbba	1	0
bbbb	0	0



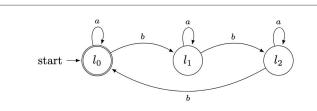
DFA that accepts strings with a number of b multiple of 3

Extended with cex

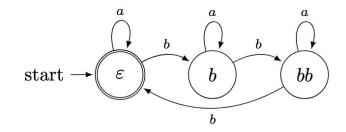
Consistent

	ε
ε	1
b	0
bb	0
bbb	1
a	1
ba	0
bba	0
bbba	1
bbbb	0

	ε	b
ε	1	0
b	0	0
bb	0	1
bbb	1	0
a	1	0
ba	0	0
bba	0	1
bbba	1	0
bbbb	0	0



DFA that accepts strings with a number of b multiple of 3



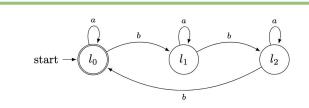
Final hypothesis

Extended with cex

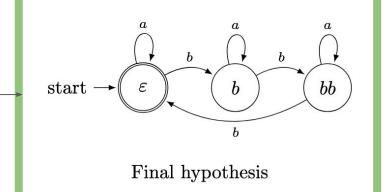
Consistent

	2 31
	ε
ε	1
b	0
bb	0
bbb	1
a	1
ba	0
bba	0
bbba	1
bbbb	0

	ε	b
ε	1	0
b	0	0
bb	0	1
bbb	1	0
a	1	0
ba	0	0
bba	0	1
bbba	1	0
bbbb	0	0



DFA that accepts strings with a number of b multiple of 3



Extended with \cos

Consistent

Correct if teacher responds correctly

- Correct if teacher responds correctly
- S contains only distinguishing states (less or equal to minimal system)

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- For every cex, at least one state added to S (loop variant)

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- S contains only distinguishing states (less or equal to minimal system)
- For every cex, at least one state added to S (loop variant)

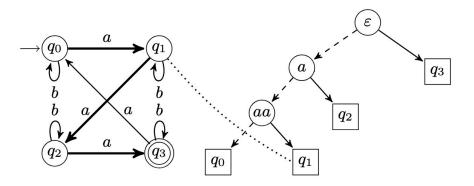
MAT: Alternative to Observation Table

Classification/Discrimination Tree

- Correct if teacher responds correctly
- S contains only distinguishing states (less or equal to minimal system)
- For every cex, at least one state added to S (loop variant)

MAT: Alternative to Observation Table

Classification/Discrimination Tree



Great! Now some issues...

Problems with MAT In Real-World Environments

Equivalence query?

Teacher vs. System?

Problems with MAT In Real-World Environments

Equivalence query?

Teacher vs. System?

Environment Noise?

Evolving System?

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Equivalence query?

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Ex.: two different answers for the same query

State of the art: cannot survive conflicts

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In practice: repeating queries so that no conflict reaches the learner

Exponential growth...

Of the number of repeats based on the probability of a conflict reaching the learner Linear increase of noise leads to an exponential increase of the number of repeats

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Exponential growth...

Of the number of repeats based on the probability of a conflict reaching the learner Linear increase of noise leads to an exponential increase of the number of repeats

If only we could allow a few conflicts...



Learner





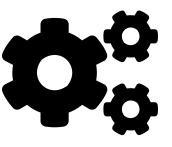
Learner



Teacher



Learner



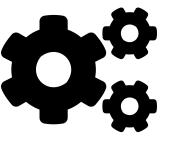
System



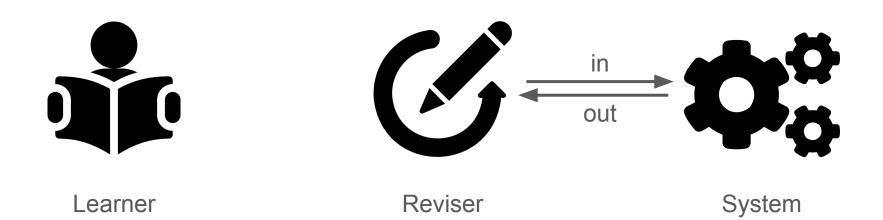
Learner



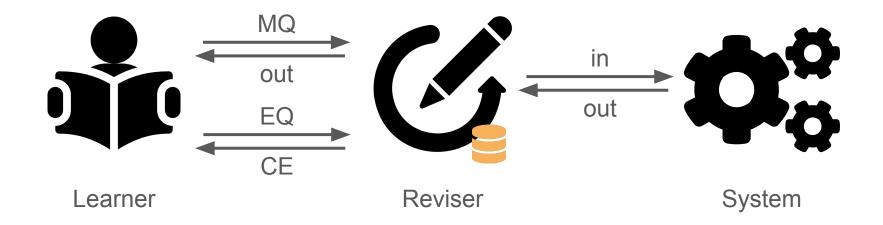
Reviser

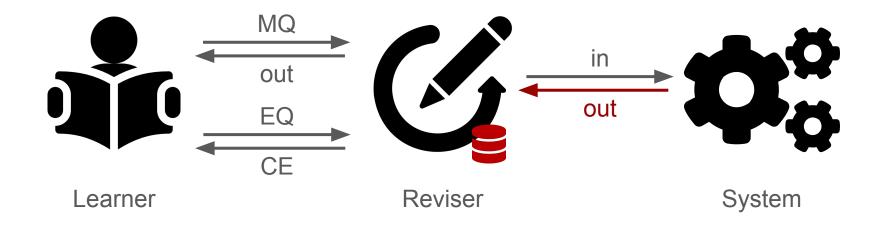


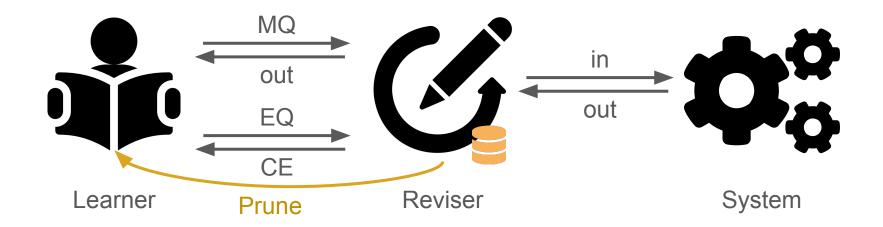
System

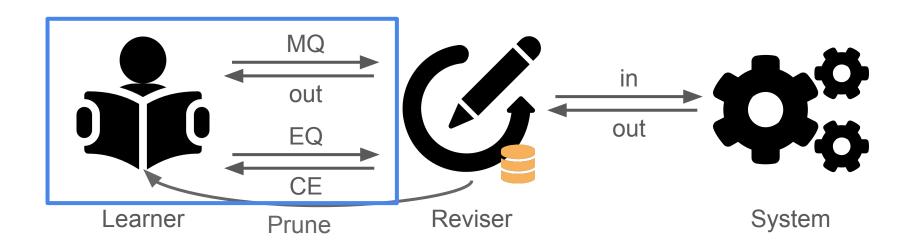












Compatible with state-of-the-art MAT Learners!

Practical Considerations

Reviser Strategy? (conflict management)

Most Recent vs. Most Frequent Answer

Practical Considerations

Reviser Strategy? (conflict management)

Most Recent vs. Most Frequent Answer

Efficiency of Prune?

No system tests during re-learning, information storage ≠ learning

- C3AL more reliable for higher levels of noise and bigger target systems
 - 96% success compared to 80% for MAT
 - noise between 0% and 0.1%
 - between 4 and 66 states
 - alphabet sizes between 7 and 22 input symbols

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 - alphabet sizes between 7 and 22 input symbols
- C3AL provides the most efficient correct model in 70% of the experiments
 - C3AL has on average a 6% reduction in the number of system tests
- We're now able to learn large systems that are noisy/evolving!



Tools

The following projects are listed in alphabetical order.

• C3AL (Conflict-Aware Active Automata Learning, link) is an alternative to the MAT framework that treats conflicts (e.g., in noisy environments) as first-class citizens. It is implemented on top of LearnLib and extends previous work on adaptive model learning.

Resources

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Thank you!